Astronomy 404 September 9, 2013

Chapter 7. Binary Systems and Stellar Parameters

Visual binary
Astrometric binary
Eclipsing binary
Spectrum binary
Spectroscopic binary

$$m_1 / m_2 = a_2 / a_1 = v_2 / v_1 = v_{2r} / v_{1r}$$
 $P^2 = \frac{4 \pi^2}{G (m_1 + m_2)} a^3$ Kepler's 3^{rd} law

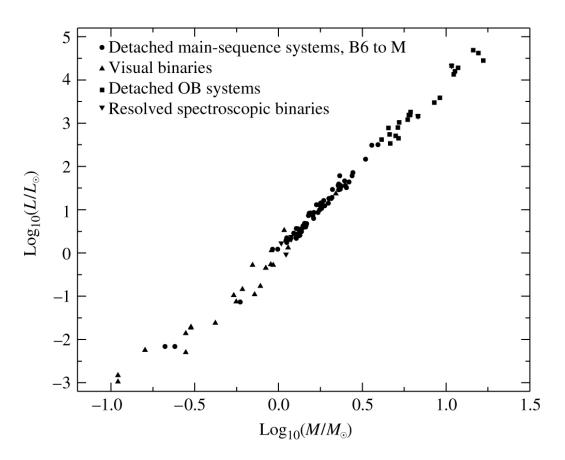
 $m_1 + m_2 \left(\text{in } M_{\odot} \right) = \frac{a^3 (\text{in AU})}{P^2 (\text{in yr})}$ Short cut

 $m_1 + m_2 = \frac{4 \pi^2}{G P^2} \frac{a^3}{\cos^3 i}$
 $m_1 + m_2 = \frac{P}{2 \pi G} \frac{(v_{1r} + v_{2r})^3}{\sin^3 i}$

To determine the total mass, both v_{1r} and v_{2r} need to be known. If only one can be measured, then

$$\frac{m_2^3}{(m_1+m_2)^2} \sin^3 i = \frac{P}{2\pi G} v_{1r}^3$$
 Mass Function (lower limit of m_2)

Mass-Luminosity Relation



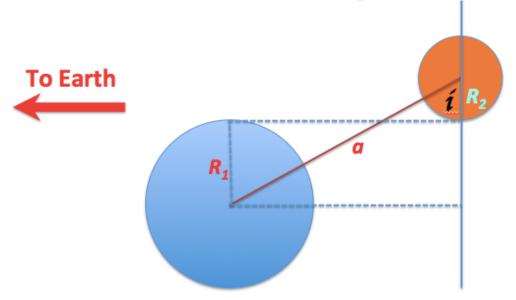
$$L \sim L_{\odot} \left(\frac{M}{M_{\odot}} \right)^5$$
 for $M \leq M_{\odot}$

$$L \sim L_{\odot} \left(\frac{M}{M_{\odot}}\right)^{3.9}$$
 for $M_{\odot} \leq M \leq 10 M_{\odot}$

$$L \sim 50 L_{\odot} \left(\frac{M}{M_{\odot}}\right)^{2.2}$$
 for $M \ge 10 M_{\odot}$

Eclipsing Binaries

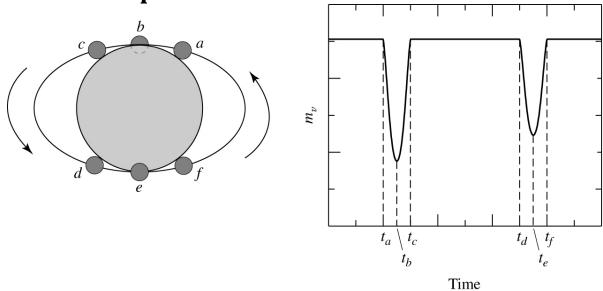
What is the minimal *i* for eclipses to occur?



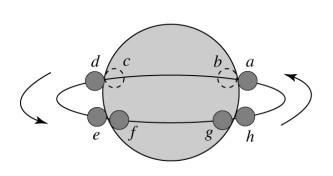
i has to be close to 90°. If *i* is 75°, $\sin^3 i = 0.90$, only 10% error in mass determination.

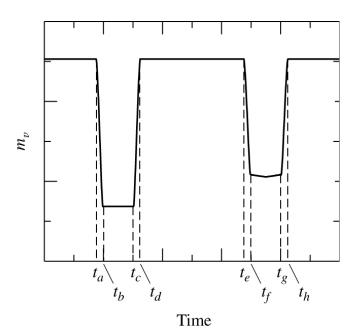
Light Curve of Eclipses

Partial eclipses



Total eclipses





$$v_s = c (\Delta \lambda_s / \lambda_0)$$

 $v_l = c (\Delta \lambda_l / \lambda_0)$

 $\Delta \lambda_s$: maximum Doppler shift of star s

 $\Delta \lambda_l$: maximum Doppler shift of star l

$$r_s = \frac{v}{2} (t_b - t_a)$$

where $v = v_s + v_l$

$$r_l = \frac{v}{2} (t_c - t_a)$$

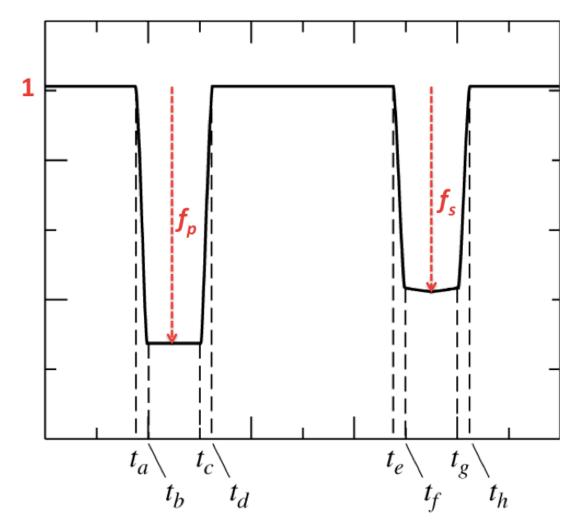
Light curve \rightarrow P, t_a , t_b , t_c ,... t_h

$$m_l/m_s = v_{rs}/v_{rl} = v_s/v_l = \Delta \lambda_s/\Delta \lambda_l$$

$$2\pi a = (v_s + v_l) P$$

$$m_l + m_s = a^3/P^2$$

 $m \text{ in } M_{\odot}$, a in AU, P in yr



Time

Total light = $\pi r_s^2 \sigma T_s^4 + \pi r_l^2 \sigma T_l^4$

$$f_p / f_s = \pi r_s^2 \sigma T_h^4 / \pi r_s^2 \sigma T_c^4 = (T_h / T_c)^4$$

But, how do we know which star is hotter? Assume star *l* is hotter,

$$f_s = \frac{\pi \, r_s^2 \, \sigma \, T_c^4}{\pi \, r_s^2 \, \sigma \, T_c^4 + \pi \, r_l^2 \, \sigma T_h^4} = \frac{1}{1 + (r_l/r_s)^2 \, (T_h/T_c)^4}$$

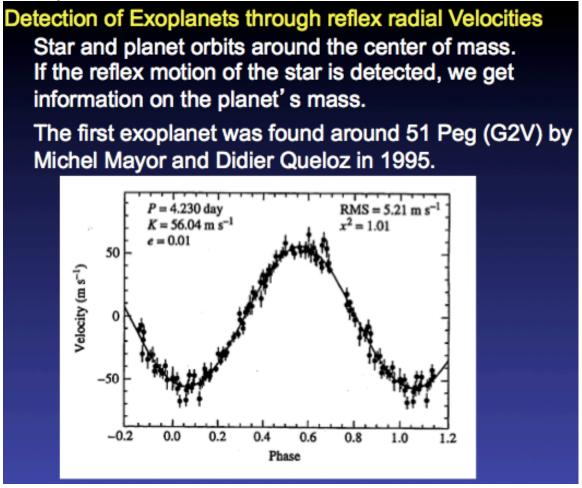
Is this f_s consistent with observation? If yes, then star l is hotter.

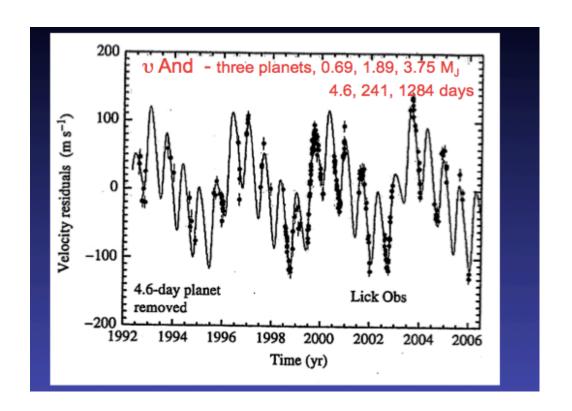
Search for Extrasolar Planets

This is a topic covered in Astr 405.

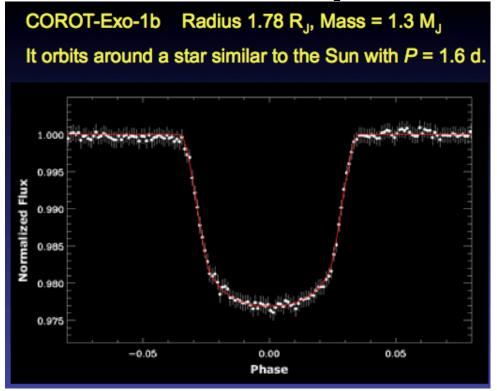
A planet orbiting around a star is just like a binary system with a large primary to secondary mass ratio.

The reflex motion of the star is small, of order of m/s. Accurate measurements are needed.





Planet transits are like eclipses.



Mercury transiting the Sun (2004)

